

# 10 PEMBEKUAN

Lecture Note  
Principles of Food Engineering (ITP 330)

Dosen :  
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PEMBEKUAN → Pengawetan pangan

Aspek engineering

- design (keperluan refrigerasi,  $\Delta T$ )
- laju pembekuan (*the rate at which freezing progress*)

Mutu produk

Produktivitas

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## PEMBEKUAN

- Penyimpanan produk pada  $T < \text{suhu beku}$
- Umumnya pada  $T < 28\text{ }^{\circ}\text{F}$  ( $-2\text{ }^{\circ}\text{C}$ ), atau khususnya pada  $< 0\text{ }^{\circ}\text{F}$  ( $-18\text{ }^{\circ}\text{C}$ )
- Sebagian besar air (~95%) beku
  - daya awet produk beku ` bbrp bulan --- tahun
  - Laju pembekuan dipengaruhi oleh bbrp faktor : perlu dikendalikan
- Pertumbuhan mikroorganisme dihambat, bbrp bahkan dirusak

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## PENGARUH PEMBEKUAN PD PROD PANGAN

### PENGARUH POSITIP

- Menurunkan/menghambat pertumbuhan m.o.
- Menurunkan laju reaksi kimia/biokimia
- Meningkatkan daya simpan produk
  - (3-40 lipat untuk setiap penurunan suhu  $10\text{ }^{\circ}\text{C}$ )

### PENGARUH NEGATIP

- Kerusakan kimia
- Kerusakan fisik (*textural*)

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### Sifat Produk Pangan Beku

- Penurunan titik didih = f (konsentrasi, BM)

$$\Delta T_f = \frac{R_g T_{A0}^2 BM_A \cdot m}{\lambda}$$

$$\Delta T_f = K \cdot m$$

↓

Lar. X dlm air  
 $T_f = (1.86 m)^\circ\text{C}$

dimana:  
 $m = \text{molalitas} \left( \frac{\text{mol solut}}{1000\text{mg pelarut}} \right)$   
 $T_{A0} = \text{titik beku pelarut murni (A)} = \text{air } (^\circ\text{K}), 273^\circ\text{K}$   
 $R_g = \text{kons tan ta gas} = 8.314 \frac{\text{J}}{\text{mol} \cdot \text{K}}$   
 $\lambda = \text{panas laten pembekuan, } \frac{\text{kJ}}{\text{kg}} \rightarrow \text{air} = 335 \frac{\text{kJ}}{\text{kg}}$   
 $BM_A = \text{Berat Molekul pelarut}$   
 $K = \text{konstanta molal titik beku}$

$$\frac{\lambda^1}{R_g} \left( \frac{1}{T_{A0}} - \frac{1}{T_A} \right) = \ln X_A \rightarrow \begin{matrix} X_A = \text{fraksi mol air} \\ \lambda^1 = \text{panas laten pembekuan} \end{matrix}$$

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### Contoh :

Ice cream mix dengan komposisi sbb:

- 10% butterfat
- 12% solid-not-fat (54.5%: laktosa)
- 15% sukrosa
- 0.22% stabilizer

---

37.22%      →      Air = 62.78%

Ditanya  $\Delta T_f = ?$       Asumsi bahwa hanya gula (laktosa+fruktosa) yang memp. Efek menurunkan titik beku) !!

$$\Delta T_f = \frac{R_g T_{A0}^2 BM_A \cdot m}{L}$$

$m = ?$       Solut? sukrosa      BM = 342

$$m = \frac{\text{mol solut}}{\text{kg solven}}$$

laktosa      BM = 342  
 solut lain diabaikan !!

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**Contoh : (lanj)**

$$\therefore \text{Fraksi gula} = 0.15 + 0.12 (0.545) = 0.2154 \text{ g/g}$$

$$\text{Fraksi air} = 0.6278$$

$$\text{Konsentrasi gula dlm air} = \frac{0.2154}{0.6278} = 0.3431 \frac{\text{g gula}}{\text{g air}}$$

$$= 343,1 \frac{\text{g gula}}{1000 \text{ g air}}$$

$$m = \frac{343,1 \text{ mol gula}}{342} = 1.003 \text{ m}$$

$$\Delta T_f = \frac{\left(8.314 \frac{\text{J}}{\text{mol.K}}\right) \left(\frac{1 \text{ mol}}{18 \text{ g}}\right) (273 \text{ K})^2 \left(18 \frac{\text{g}}{\text{mol}}\right) \left(1.003 \frac{\text{mol}}{\text{kg}}\right)}{1000.335 \frac{\text{J}}{\text{kg}}}$$

$$\Delta T_f = 1,86 \text{ K}$$

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**Panas Laten Pembekuan**

$$\text{Air murni } \lambda = 335 \frac{\text{kJ}}{\text{kg}}$$

$$\text{Larutan solid x dlm air } \lambda = (335 m_w) \frac{\text{kJ}}{\text{kg}}$$

$$m_w = \text{Fraksi massa air}$$

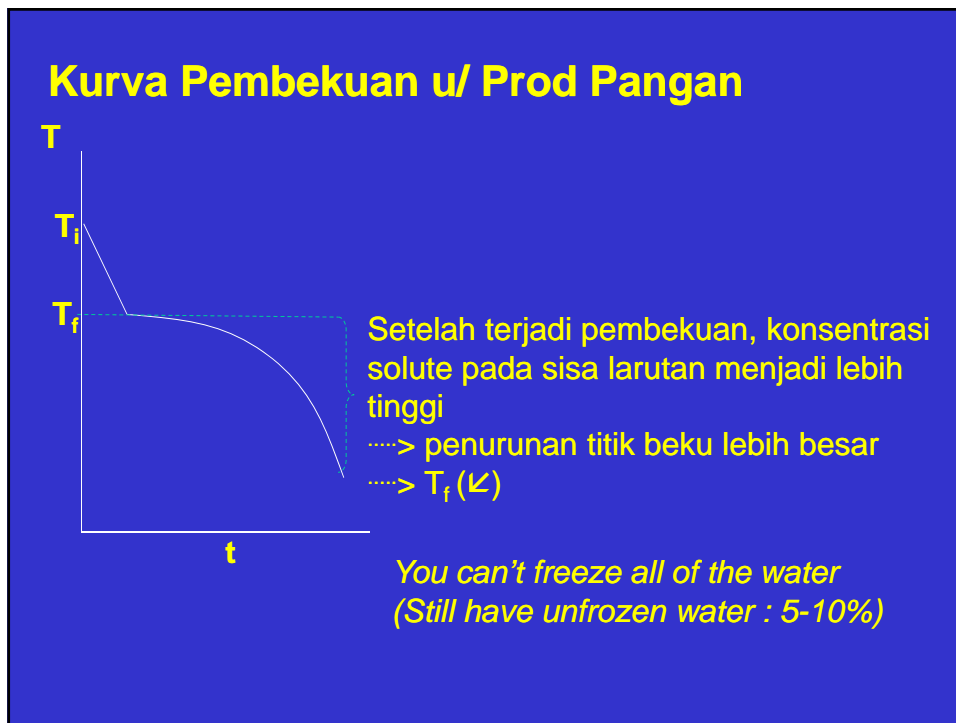
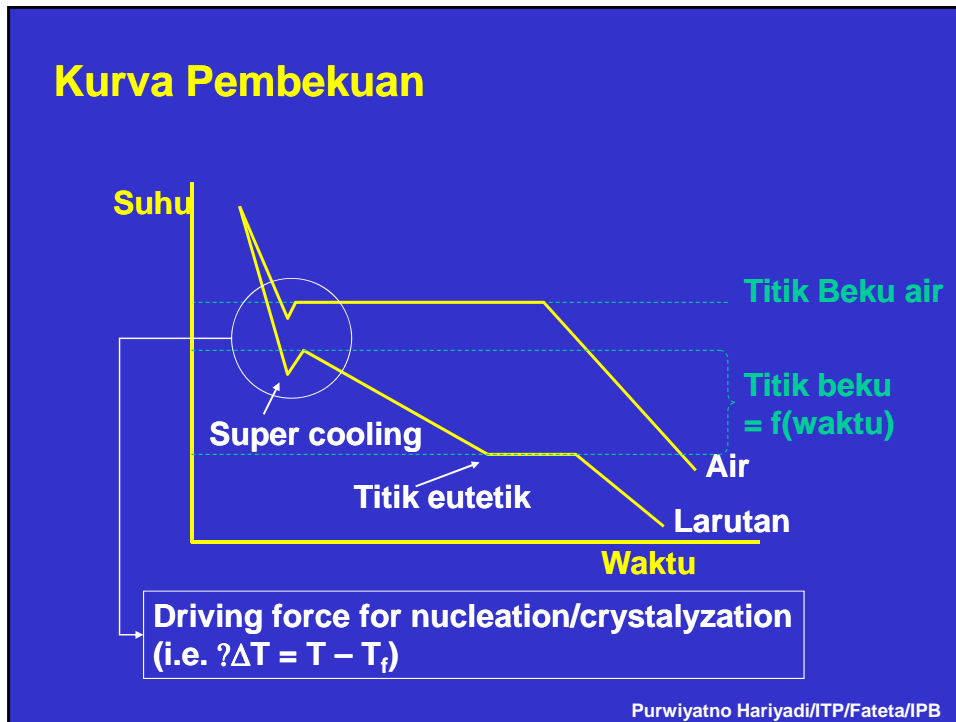
Contoh:

|                           | Kadar air | $\lambda \left(\frac{\text{kJ}}{\text{kg}}\right)$ |                                    |
|---------------------------|-----------|--|------------------------------------|
| Selada                    | 94.8      | 316.3 (317.6)                                      | } Perhitungan berdasarkan pd rumus |
| Strawberi                 | 90.8      | 289.6 (304.5)                                      |                                    |
| Kacang panjang            | 88.9      | 297.0 (297.8)                                      |                                    |
| Kentang                   | 77.8      | 258.0 (260.0)                                      |                                    |
| Daging kambing            | 58.0      | 194.0 (194.3)                                      |                                    |
| Kacang merah, biji kering | 12.5      | 41.9 (41.9)  |                                    |
| Kurma kering              | 24.0      | 79.0 (80.4)  |                                    |

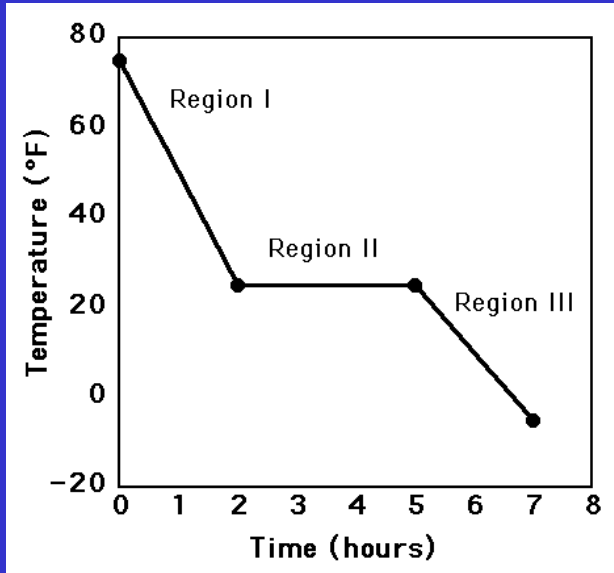
$$\text{Air: } \lambda = 335 \frac{\text{kJ}}{\text{kg}} = \frac{335 \cdot 10^3 \text{ J}}{\text{kg}} \left(\frac{18 \cdot 10^{-3}}{1 \text{ mol}}\right)$$

$$\lambda = 6030 \frac{\text{J}}{\text{mol}}$$

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**FREEZING OF WATER**

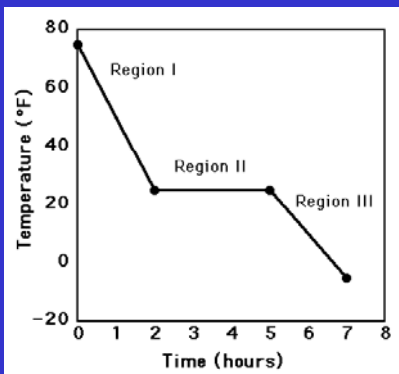


T-t Diagram :

A schematic freezing curve for water, displaying sensible heat loss (Regions I and III) and latent heat loss (Region II).

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**ENERGY REMOVAL ASSOCIATED WITH FREEZING**



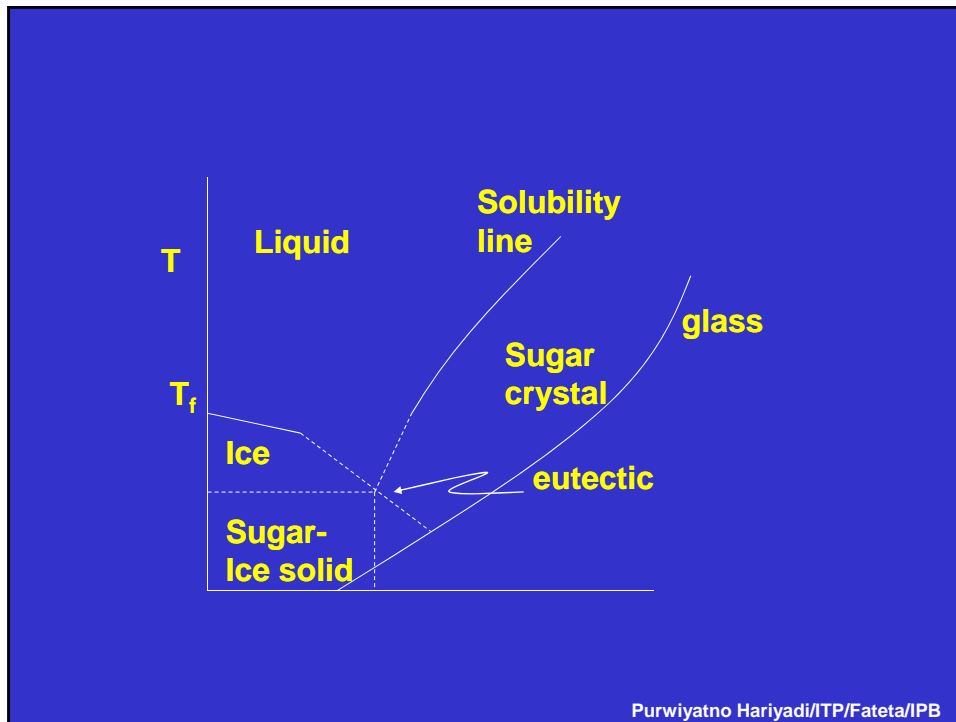
Removal of heat (Q) from Region I (sensible heat), II (latent heat), and III (sensible heat) :

(1)  $Q_1 = mC_{p1}\Delta T_1$   
 $m$  = weight of food  
 $C_{p1}$  = specific heat of food above freezing  
 $\Delta T$  = temperature difference

(2)  $Q_2 = m_w \lambda$  .....>  $m_w$  = weight of water  
 .....>  $\lambda$  = latent heat

(3)  $Q_3 = mC_{p2}\Delta T_3$  .....>  $m$  = weight of food  
 .....>  $C_{p2}$  = specific heat of frozen food  
 .....>  $\Delta T_3$  = temperature difference

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**INITIAL FREEZING TEMPERATURE**

Buah anggur (grape) .....> kadar air 84.7%  
 .....> T<sub>f</sub> = -1.8°C (271.2K)

$$\frac{\lambda^1}{R_g} \left( \frac{1}{T_{A0}} - \frac{1}{T_A} \right) = \ln X_A$$

$\lambda^1 = 6003 \frac{\text{J}}{\text{mol}}$   
 $R_g = 8.314 \frac{\text{J}}{\text{mol} \cdot \text{K}}$

X<sub>A</sub>=?

$$\frac{6003 \frac{\text{J}}{\text{mol}}}{8,314 \frac{\text{J}}{\text{mol} \cdot \text{K}}} \left( \frac{1}{273\text{K}} - \frac{1}{271.2\text{K}} \right) = \ln X_A$$

Ln X<sub>A</sub> = - 0.01755

X<sub>A</sub> = 0.9826 (effective mol fraction of water)      $\frac{\text{m grape}}{\text{ml}}$

### INITIAL FREEZING TEMPERATURE

$$X_A = \text{fraksi mol air} = 0.9826$$

$$X_A = 0.9826 = \frac{\frac{84.7}{18}}{\frac{84.7}{18} + \frac{15.3}{BM_E}}$$

$$BM_E = 183.61$$

Juice anggur dapat dianggap bertingkah laku mirip/sama dgn

- lar. x dlm air
- $BM_x = 183.61 \frac{\text{mol}}{\text{g}}$
- $X_A = 0.9826$
- $X_x = \dots\dots\dots \text{dst}$

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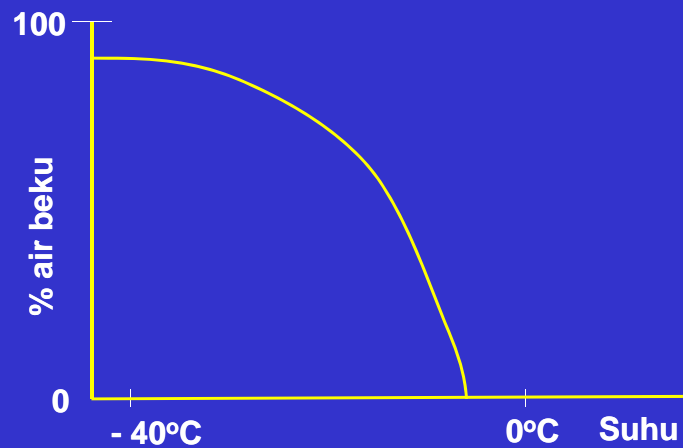
### PERHITUNGAN PEMBEKUAN (DESIGN)

- Pendugaan keperluan pembekuan
  - ? ukuran sistem "mechanical compression"
  - ? evaluasi beban refrigerasi/pembekuan
- Disain peralatan + proses, untuk :
  - ? memperoleh pembekuan yg diinginkan
    - koef pindah panas
    - laju pembekuan

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### Hubungan antara % air beku vs. suhu



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### LAJU PEMBEKUAN

- EQUIPMENT RELATED
  - rate of heat transfer
  - size of refrigeration unit
- FOOD/PRODUCT QUALITY
  - slow freezing
    - result in formation of few, large ice crystals
    - damaging to cell structure/quality
  - rapid freezing
    - results in many small ice crystals
    - gives best product quality
    - leads to IQF techniques
- water .....> ice: ~ 9% increase in volume

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## FREEZING TIME

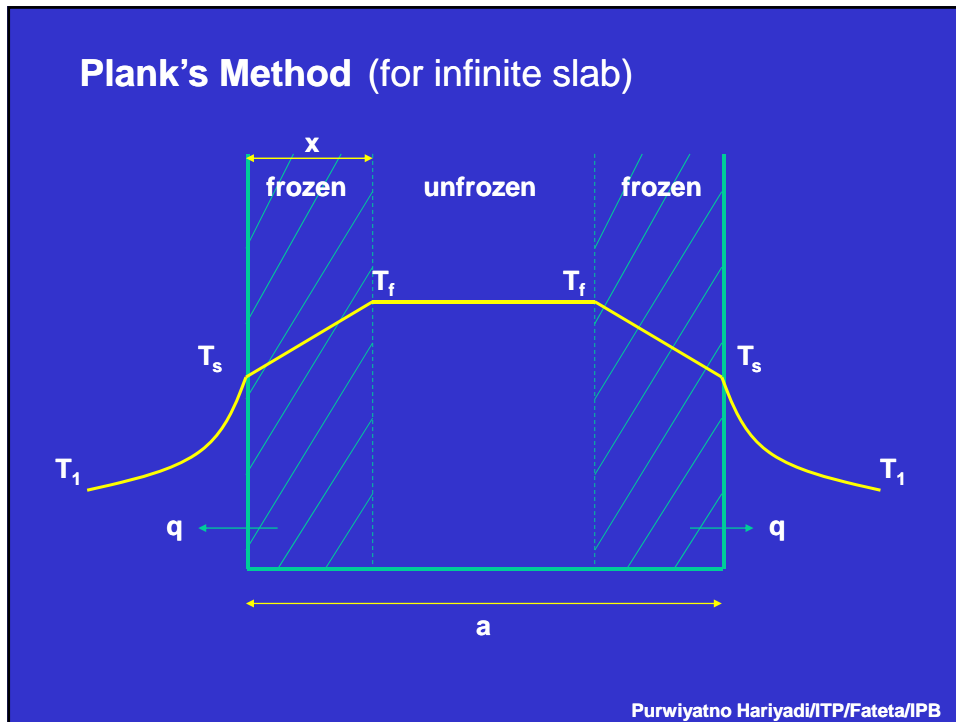
- Time-temperature method +
    - Time required to freeze between two temperatures (usually  $T = -5^{\circ}\text{C}$  or  $-10^{\circ}\text{C}$ )
  - Velocity of ice front
    - rate of freezing
    - must be able to see ice front
  - Appearance of specimen
    - internal conditions
  - Thermal methods
    - calorimetric techniques
    - not real-world condition
- + *Time-temp. methods most common*  
+ *many people use time to freeze to  $-10^{\circ}\text{C}$  as standard.*

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## PERHITUNGAN WAKTU PEMBEKUAN

- panas laten adalah energi utama yang hrs diperhitungkan pada proses pembekuan
  - ~ 75% total energi pd proses pembekuan
    - 333.3 kJ/kg air
    - 144 BTU/lb air
- Terjadi perubahan sifat fisik bahan selama proses pembekuan  $\sim f(T, m)$

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### Plank's Method (for infinite slab)

Convection:

$$q \left( \frac{\text{BTU}}{\text{hr}} \right) = Qt = hA (T_f - T_1) \dots\dots \text{Pers. 1}$$

$h$  = convective heat transfer coeff. at the product surface.

Conduction:

$$q = \frac{k_f \cdot A}{x} (T_f - T_s) \dots\dots \text{Pers. 2}$$

$T_f$  = initial freezing point  
 $x = x(t)$

Combine 1&2:

$$q = \frac{(T_f - T_1)}{\frac{x}{k_f} + \frac{1}{h}} \dots\dots \text{Pers. 3}$$

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**Plank's Method (for infinite slab)**

Jumlah energi yang dibebaskan selama proses pembekuan

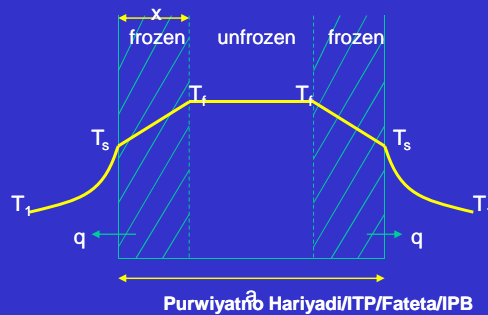
$$qdt = m_i \lambda_f = \rho_f dV \lambda_f$$

$$qdt = \rho_f \lambda_f A dx$$

so,  $q = \rho_f \lambda_f A dx/dt$  ..... Pers. 4

Ingat Pers 3 :

$$q = \frac{(T_f - T_i)A}{\frac{x}{k_f} + \frac{1}{h}}$$



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**Plank's Method (for infinite slab)**

Kombinasi Pers. 3 dan 4 .....>

$$\rho_f \lambda_f A \frac{dx}{dt} = \frac{(T_f - T_i)A}{\frac{x}{k_f} + \frac{1}{h}}$$

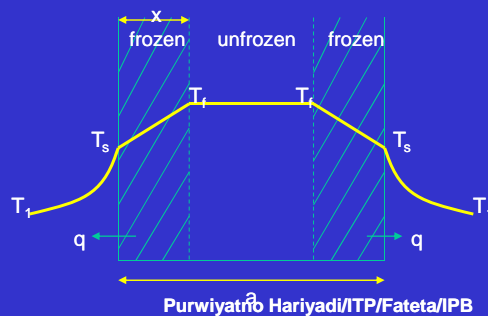
Pembekuan selesai lempeng jika  $x = a/2$

$$\rho_f \lambda_f \left( \frac{x}{k_f} + \frac{1}{h} \right) dx = (T_f - T_i) dt$$

$$\rho_f \lambda_f \int_0^{a/2} \left[ \frac{x}{k_f} + \frac{1}{h} \right] dx = (T_f - T_i) \int_0^{t_f} dt$$

$$t_f = \frac{\rho_f \lambda_f}{T_f - T_i} \left[ \frac{a^2}{8k} + \frac{a}{2h} \right]$$

$T_i$  = Suhu Pembekuan  
Suhu ruang pembeku



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## GENERAL FLANKS EQUATION

$$t_f = \frac{\rho_f \lambda_f}{(T_f - T_i)} \left[ \frac{Ra^2}{k_f} + \frac{Pa}{n} \right]$$

Where:

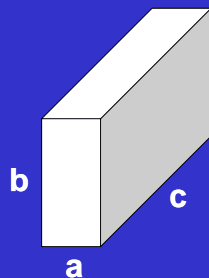
|   | Infinite slab | Sphere   | Infinite cylinder | Cube |
|---|---------------|----------|-------------------|------|
| P | 1/2           | 1/6      | 1/4               | 1/8  |
| R | 1/8           | 1/24     | 1/6               | 1/24 |
| a | Thickness     | Diameter | Diameter          | Edge |

$$\lambda_f = \text{latent heat of fusion [=} \frac{\text{kJ}}{\text{kg}}$$

$$\lambda_{\text{water}} = 333.22 \frac{\text{kJ}}{\text{kg}} = 144 \frac{\text{BTU}}{\text{lb}}$$

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## GENERAL FLANKS EQUATION



P dan R untuk bentuk bata

a : dimensi terpendek

c : dimensi terpanjang

$$B_2 = c/a$$

$$B_1 = b/a$$

Lihat chart/diagram :

dengan diketahui nilai  $B_2$  dan  $B_1$  maka dapat dibaca nilai P dan R

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Limitation of Plank's method:

- no superheating or supercooling
- thermal properties are constant
- can't incorporate a variable heat transfer coeff.
- can't handle varying freezing point

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Selesai .....

Sekarang ke.....

Psikrometrik